

Mathematics  
PAPER 1 (Non-Calculator)  
Higher Tier

Total Marks
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Thursday 16 May 2024 – Morning

Time: 1 hour 30 minutes

In the boxes below, write your name, centre number and candidate number.

Surname					
Other names					
Centre Number					
Candidate Number					

## **YOU MUST HAVE**

**Ruler, protractor, pair of compasses, writing and drawing equipment, Formulae Booklet (enclosed). Tracing paper may be used.**

## **YOU WILL BE GIVEN**

**A separate Diagram Booklet**

## **INSTRUCTIONS**

**Answer ALL questions.**

**Answer the questions in the spaces provided in this Question Paper or in the separate Diagram Booklet – there may be more space than you need.**

**You must show all your working.**

**Diagrams are NOT accurately drawn, unless otherwise indicated.**

**Calculators may not be used.**

**You may be given cut out shapes for Question 11.**

**Turn over**

## **INFORMATION**

**The total mark for this paper is 80**

**The marks for EACH question are shown in brackets – use this as a guide as to how much time to spend on each question.**

**There may be spare copies of some diagrams.**

## **ADVICE**

**Read each question carefully before you start to answer it.**

**Try to answer every question.**

**Check your answers if you have time at the end.**



**Answer ALL questions.**

**Write your answers in the spaces provided.**

**You must write down all the stages in your working.**

1. Here are the first four terms of an arithmetic sequence.

1

5

9

13

Find an expression, in terms of  $n$ , for the  $n$ th term of this sequence.

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**(Total for Question 1 is 2 marks)**

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**Turn over**

2. (a) Work out  $3\frac{4}{5} - 1\frac{2}{3}$   
(2 marks)

**2. continued.**

**(b) Kevin was asked to work out  $2\frac{1}{3} \times \frac{5}{8}$**

**Here is his working and his answer.**

$$2\frac{1}{3} \times \frac{5}{8} = \frac{7}{3} \times \frac{5}{8}$$

$$= \frac{35}{24}$$

$$= 1\frac{9}{24}$$

**Kevin's answer is wrong.**

**What mistake has Kevin made?**

**(1 mark)**

**Answer space continues on the next page.**

**Turn over**

**2. (b) continued.**

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**(Total for Question 2 is 3 marks)**

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**3. Look at the diagram for Question 3 in the separate Diagram Booklet.**

**The diagram is NOT accurately drawn.**

**The diagram shows a plan of a floor labelled **ABCDEF**.**

**In the diagram:**

**$AB = 10 \text{ m}$**

**$BC = 5 \text{ m}$**

**$EF = 6 \text{ m}$**

**$FA = 8 \text{ m}$**

**Petra is going to cover the floor with paint.**

**Petra has 3 tins of paint.**

**There are 2.5 litres of paint in each tin.**

**Petra thinks 1 litre of paint will cover  $10 \text{ m}^2$  of floor.**

**(continued on the next page)**

**Turn over**

**3. continued.**

- (a) Assuming Petra is correct, does she have enough paint to cover the floor?  
You must show all your working.  
(4 marks)**

**Answer space continues on the next page.**

**3. (a) continued.**

**(continued on the next page)**

**Turn over**

**3. continued.**

**(b) Actually, 1 litre of paint will cover  
11 m<sup>2</sup> of floor.**

**Does this affect your answer  
to part (a)?**

**You must give a reason for  
your answer.**

**(1 mark)**

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**(Total for Question 3 is 5 marks)**

**Turn over**

**4. Look at the diagram for Question 4 in the separate Diagram Booklet.**

**The diagram shows a Venn diagram with Set P and Set Q.**

**(a) Write down the numbers that are in set  $P'$**

**(1 mark)**

**4. continued.**

**(b) A number is chosen at random from the universal set,  $\mathcal{E}$**

**Find the probability that this number is in the set  $P \cup Q$   
(2 marks)**

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**(Total for Question 4 is 3 marks)**

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**Turn over**

5. (a) Sophie drives a distance of 513 kilometres on a motorway in France. She pays 0.81 euros for every 10 kilometres she drives.

Work out an estimate for the total amount that Sophie pays.

(3 marks)

\_\_\_\_\_ euros

**5. continued.**

**(b) Is your answer to part (a) an underestimate or an overestimate?**

**Give a reason for your answer.**

**(1 mark)**

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**(Total for Question 5 is 4 marks)**

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**Turn over**

- 6. (a) Look at the diagram for Question 6 in the separate Diagram Booklet.**

**The diagram shows a straight line L drawn on a coordinate grid.**

**Find an equation for L.**

**(3 marks)**

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**(continued on the next page)**

**6. continued.**

**(b) M is a different straight line with  
equation  $y = 5x$**

**Write down the equation of a straight  
line parallel to M.**

**(1 mark)**

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**(Total for Question 6 is 4 marks)**

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7. Kasim has some small jars, some medium jars and some large jars. He has a total of 400 jars.

$\frac{3}{8}$  of the 400 jars are empty.

For the empty jars,

number of small jars : number of medium jars = 3 : 4

number of medium jars : number of large jars = 1 : 2

Work out the percentage of Kasim's jars that are empty small jars.

(5 marks)

Answer space continues on the next 2 pages.

**7. continued.**

**7. continued.**

\_\_\_\_\_ %

**(Total for Question 7 is 5 marks)**

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**Turn over**

**8. Len has 8 parcels.**

**The mean weight of the 8 parcels  
is 2.5 kg**

**The mean weight of 3 of the parcels  
is 2 kg**

**Work out the mean weight of the  
other 5 parcels.**

**(3 marks)**

**Answer space continues on the next page.**

8. continued.

\_\_\_\_\_ kg

**(Total for Question 8 is 3 marks)**

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9. In a sale, the normal price of a coat is reduced by  $R\%$

Given that

$$\text{sale price} = 0.7 \times \text{normal price}$$

find the value of  $R$

$R =$  \_\_\_\_\_

(Total for Question 9 is 1 mark)

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Turn over

**10. Solve the simultaneous equations**

$$5x - 2y = 23$$

$$2x - 3y = 18$$

**(4 marks)**

**Answer space continues on the next page.**

**10. continued.**

**x = \_\_\_\_\_**

**y = \_\_\_\_\_**

**(Total for Question 10 is 4 marks)**

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**Turn over**

**11. Look at the diagram for Question 11 in the separate Diagram Booklet.**

**The diagram shows Triangle A on a coordinate grid.**

**You may be given cut out shapes for this question.**

**Triangle A is translated by the**

**vector  $\begin{pmatrix} 6 \\ -4 \end{pmatrix}$  to give Triangle B.**

**Triangle B is rotated  $90^\circ$  clockwise about the point  $(1, 1)$  to give Triangle C.**

**Describe fully the single transformation that maps Triangle A onto Triangle C.**

**(3 marks)**

**Answer space continues on the next page.**

**Turn over**

**11. continued.**

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**(Total for Question 11 is 3 marks)**

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**12. Look at the diagram for Question 12 in the separate Diagram Booklet.**

**The diagram shows nine graphs labelled A, B, C, D, E, F, G, H, and J.**

**Write down the letter of the graph that could have the equation**

**(i)  $y = x^2 - 4$**   
**(1 mark)**

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**(continued on the next page)**

**12. continued.**

**Write down the letter of the graph that could have the equation**

**(ii)  $y = -x^3$**   
**(1 mark)**

\_\_\_\_\_

**(iii)  $y = -\frac{5}{x}$**   
**(1 mark)**

\_\_\_\_\_

**(Total for Question 12 is 3 marks)**

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**Turn over**

- 13. The table below gives information about the amount of time that each of 150 people were in a shop.**

<b>Time (<math>t</math> minutes)</b>	<b>Frequency</b>
<b><math>0 &lt; t \leq 10</math></b>	<b>20</b>
<b><math>10 &lt; t \leq 30</math></b>	<b>70</b>
<b><math>30 &lt; t \leq 35</math></b>	<b>20</b>
<b><math>35 &lt; t \leq 50</math></b>	<b>30</b>
<b><math>50 &lt; t \leq 60</math></b>	<b>10</b>

- (a) Look at the diagram for Question 13(a) in the separate Diagram Booklet.**
- The diagram shows a grid.**
- On the grid, draw a histogram for this information.**
- (3 marks)**

**(continued on the next page)**

**Turn over**

**13. continued.**

<b>Time (t minutes)</b>	<b>Frequency</b>
<b><math>0 &lt; t \leq 10</math></b>	<b>20</b>
<b><math>10 &lt; t \leq 30</math></b>	<b>70</b>
<b><math>30 &lt; t \leq 35</math></b>	<b>20</b>
<b><math>35 &lt; t \leq 50</math></b>	<b>30</b>
<b><math>50 &lt; t \leq 60</math></b>	<b>10</b>

**(b) Work out an estimate for the fraction of these 150 people who were in the shop for between 20 minutes and 40 minutes.  
(2 marks)**

**Answer space continues on the next page.**

**Turn over**

13. (b) continued.

Time (t minutes)	Frequency
$0 < t \leq 10$	20
$10 < t \leq 30$	70
$30 < t \leq 35$	20
$35 < t \leq 50$	30
$50 < t \leq 60$	10

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(Total for Question 13 is 5 marks)

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Turn over

**14. Expand and simplify**

$$(3x - 1)(2x + 3)(x - 5)$$

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**(Total for Question 14 is 3 marks)**

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**Turn over**

**15. Look at the diagram for Question 15 in the separate Diagram Booklet.**

**The diagram is NOT accurately drawn.**

**The diagram shows a sector of a circle labelled  $OAB$ , with centre  $O$  and radius 6 cm**

**$OA = 6$  cm**

**$OB = 6$  cm**

**The length of the arc  $AB$  is  $5\pi$  cm**

**Work out, in terms of  $\pi$ , the area of the sector.**

**Give your answer in its simplest form.**

**(4 marks)**

**Answer space continues on the next page.**

**15. continued.**

\_\_\_\_\_  $\text{cm}^2$

**(Total for Question 15 is 4 marks)**

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**Turn over**

**16. There are only  $n$  orange sweets and 1 white sweet in a bag.**

**Saira takes at random a sweet from the bag and eats the sweet.**

**She then takes at random another sweet from the bag and eats this sweet.**

**Show that the probability that Saira eats two orange sweets is  $\frac{n-1}{n+1}$**

**(2 marks)**

**Answer space continues on the next page.**

**16. continued.**

**(Total for Question 16 is 2 marks)**

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**Turn over**

17. (a) Rationalise the denominator of  $\frac{1}{\sqrt{7}}$   
(1 mark)

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(continued on the next page)

**17. continued.**

**(b) Simplify fully  $\sqrt{80} - \sqrt{5}$**   
**(2 marks)**

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**(Total for Question 17 is 3 marks)**

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**Turn over**

18. Show that  $0.\dot{1}\dot{5} + 0.\dot{2}\dot{2}\dot{7}$  can be written in the form  $\frac{m}{66}$  where  $m$  is an integer.  
(3 marks)

Answer space continues on the next 2 pages.

**18. continued.**

**18. continued.**

**(Total for Question 18 is 3 marks)**

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**Turn over**

**19. Look at the diagram for Question 19 in the separate Diagram Booklet.**

**The diagram is NOT accurately drawn.**

**The diagram shows two similar isosceles triangles,  $ABC$  and  $DAB$ .**

$$AB = AC$$

$$AD = BD$$

$$BC : CD = 4 : 21$$

**Find the ratio  $AB : AD$**

**(3 marks)**

**Answer space continues on the next page.**

**19. continued.**

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**(Total for Question 19 is 3 marks)**

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**Turn over**

20.  $2^x = \frac{2^n}{\sqrt[3]{2}}$        $2^y = (\sqrt{2})^5$

Given that  $x + y = 8$

work out the value of  $n$ .

Answer space continues on the next page.

**20. continued.**

**n = \_\_\_\_\_**

**(Total for Question 20 is 3 marks)**

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**Turn over**

**21. A solid cuboid has a volume of  $300 \text{ cm}^3$   
The cuboid has a total surface area  
of  $370 \text{ cm}^2$**

**The length of the cuboid is  $20 \text{ cm}$   
The width of the cuboid is greater  
than the height of the cuboid.**

**Work out the height of the cuboid.  
You must show all your working.  
(5 marks)**

**Answer space continues on the next 2 pages.**

**21. continued.**

**21. continued.**

\_\_\_\_\_ cm

**(Total for Question 21 is 5 marks)**

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**Turn over**

- 22. (a) Look at the diagram for Question 22 in the separate Diagram Booklet. The diagram shows two axes. On the axes, sketch the graph of  $y = \sin x^\circ$  for  $0 \leq x \leq 360$  (2 marks)**

**(continued on the next page)**

**22. continued.**

**(b) Solve the equation below**

$$2 \sin x^\circ = -1 \text{ for } 0 \leq x \leq 360$$

**(2 marks)**

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**(Total for Question 22 is 4 marks)**

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**Turn over**

**23. C is a circle with centre  $(0, 0)$**

**L is a straight line.**

**The circle C and the line L intersect at the points P and Q.**

**The coordinates of P are  $(5, 10)$**

**The X coordinate of Q is  $-2$**

**L has a positive gradient and crosses the y-axis at the point  $(0, k)$**

**Find the value of k.**

**(5 marks)**

**Answer space continues on the next 2 pages.**

**23. continued.**

**23. continued.**

**k = \_\_\_\_\_**

**(Total for Question 23 is 5 marks)**

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**TOTAL FOR PAPER IS 80 MARKS**

**END OF PAPER**

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